

Lecture 5. Anisotropy decay/data analysis

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- Anisotropy decay
- Energy-transfer distance distributions
- Time resolved spectra
- Excited-state reactions

Basic physics concept in polarization

The probability of emission along the x (y or z) axis depends on the orientation of the transition dipole moment along a given axis.

If the orientation of the transition dipole of the molecule is **changing**, the measured fluorescence intensity along the different axes **changes** as a function of time.

Changes can be due to:

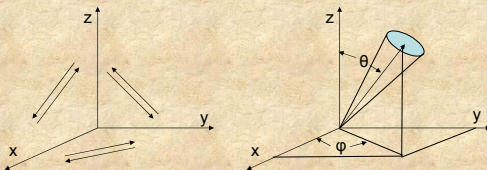
- Internal conversion to different electronic states
- changes in spatial orientation of the molecule
- energy transfer to a fluorescence acceptor with different orientation

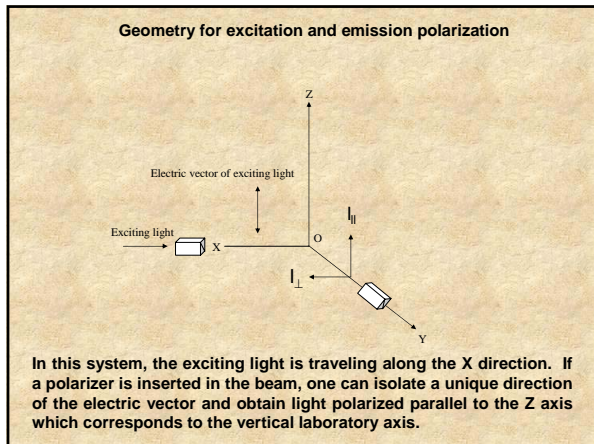
Anisotropy Decay

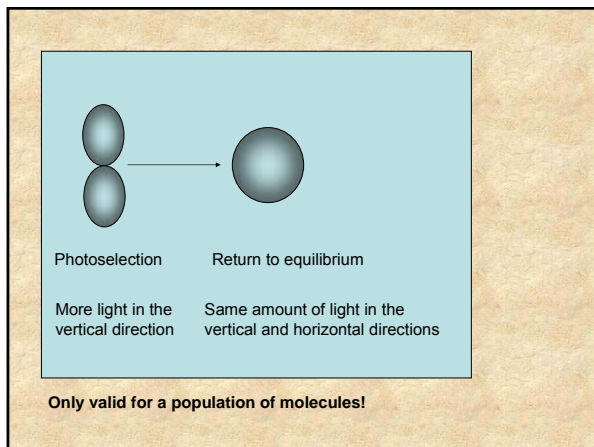
Transfer of emission from one direction of polarization to another

Two different approaches

- Exchange of orientation among fixed directions
- Diffusion of the orientation vector





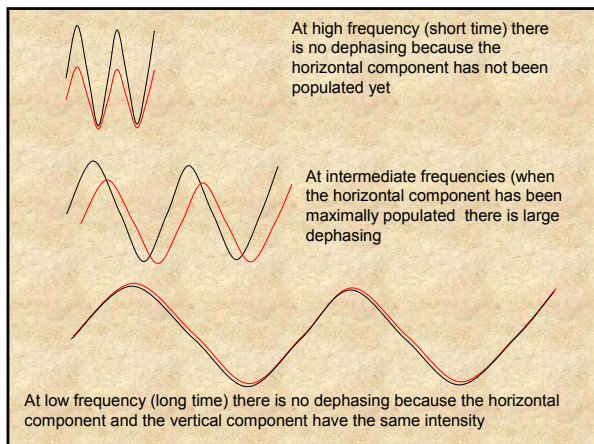


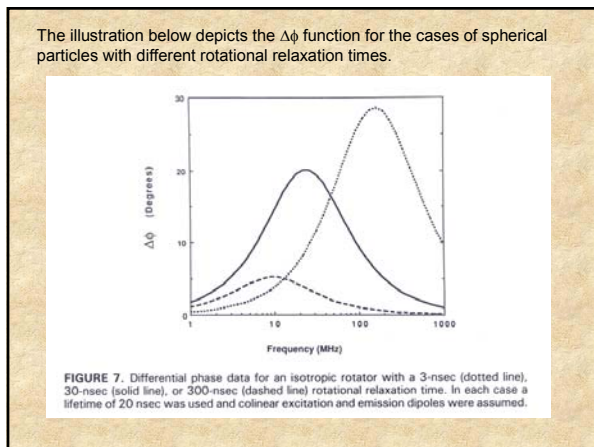
Time-resolved methodologies measure the changes of orientation as a function of time of a system. The time-domain approach is usually termed the **anisotropy decay** method while the frequency-domain approach is known as **dynamic polarization**. Both methods yield the same information.

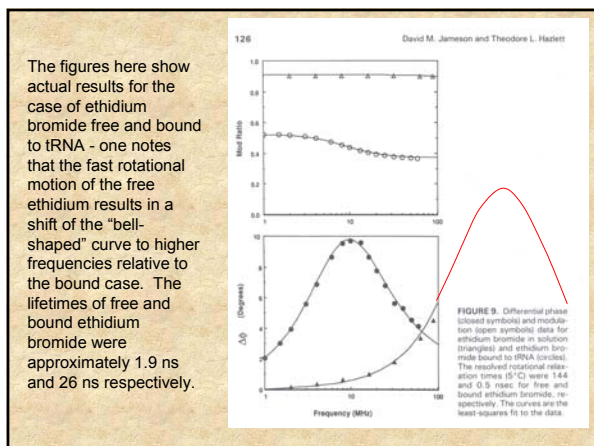
In the time-domain method the sample is illuminated by a pulse of vertically polarized light and the decay over time of both the vertical and horizontal components of the emission are recorded. The anisotropy function is then plotted versus time as illustrated here:

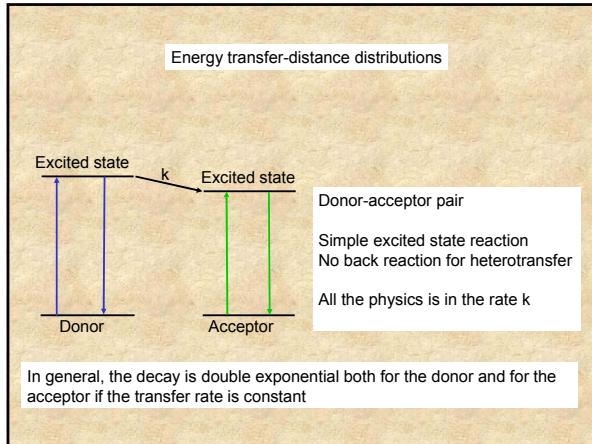
The decay of the anisotropy with time (r) for a sphere is then given by:

$$r = \frac{I_V - I_H}{I_V + 2 I_H} = r_o e^{-(t/\tau_c)}$$









The rate of transfer (k_T) of excitation energy is given by:

$$k_T = (1/\tau_d)(R_0/R)^6$$

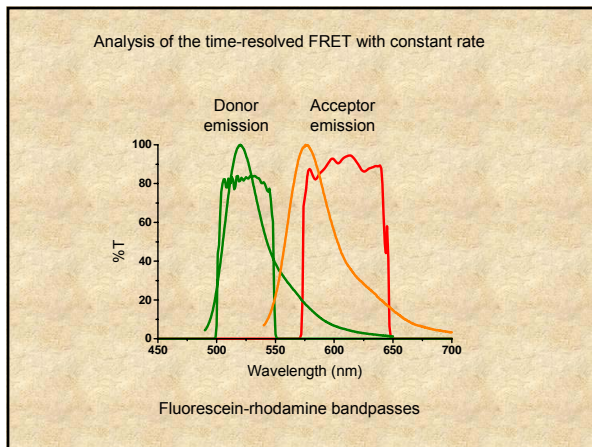
Where τ_d is the fluorescence lifetime of the donor in the absence of acceptor, R the distance between the centers of the donor and acceptor molecules and R_0 is defined by:

$$R_0 = 0.211(n^{-4}Q_d\kappa^2J)^{1/6} \text{ \AA}$$

Where n is the refractive index of the medium (usually between 1.2-1.4), Q_d is the fluorescence quantum yield of the donor in absence of acceptor, κ^2 is the orientation factor for the dipole-dipole interaction and J is the normalized spectral overlap integral. [$\epsilon(\lambda)$ is in $M^{-1} \text{ cm}^{-1}$, λ is in nm and J are $M^{-1} \text{ cm}^{-1} (\text{nm})^4$]

R_0 is the Förster critical distance at which 50% of the excitation energy is transferred to the acceptor and can be approximated from experiments independent of energy transfer.

In principle, the distance R for a collection of molecules is variable and the orientation factor could also be variable



General expressions for the decay
Hetero-transfer; No excitation of the donor

$$I_D = a_d e^{-k_1 t} - b_d e^{-k_2 t}$$

Intensity decay as measured at the donor bandpass

$$I_A = a_a e^{-k_1 t} - b_a e^{-k_2 t}$$

Intensity decay as measured at the acceptor bandpass

$$k_1 = \Gamma_a + k_t \quad k_2 = \Gamma_d$$

$$a_d = -B_a k_t \quad b_d = B_d (\Gamma_a - \Gamma_d - k_t)$$

$$a_a = B_a (\Gamma_a - \Gamma_d) - B_d k_t \quad b_a = -B_a (\Gamma_a - \Gamma_d)$$

Γ_d and Γ_a are the decay rates of the donor and acceptor.
 B_d and B_a are the relative excitation of the donor and of the acceptor.
 The total fluorescence intensity at any given observation wavelength is given by

$$I(t) = SAS_d I_d(t) + SAS_a I_a(t)$$

where SAS_d and SAS_a are the relative emission of the donor and of the acceptor, respectively.

If the rate k_t is **distributed**, for example because in the population there is a distribution of possible distances, then we need to add all the possible values of the distance weighted by the proper distribution of distances

Example (in the time domain) of gaussian distribution of distances

(Next figure)

If the distance changes during the decay (dynamic change) then the starting equation is no more valid and different equations must be used (Beechem and Hass)

FRET-decay, discrete and distance gaussian distributed
 Question: Is there a "significant" difference between one length and a distribution of lengths?

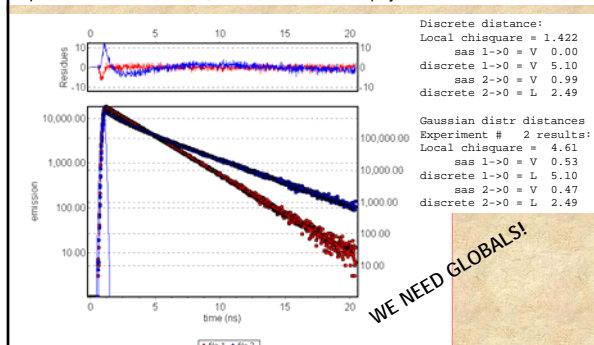
Clearly the fit distinguishes the two cases if we ask the question: what is the width of the length distribution?

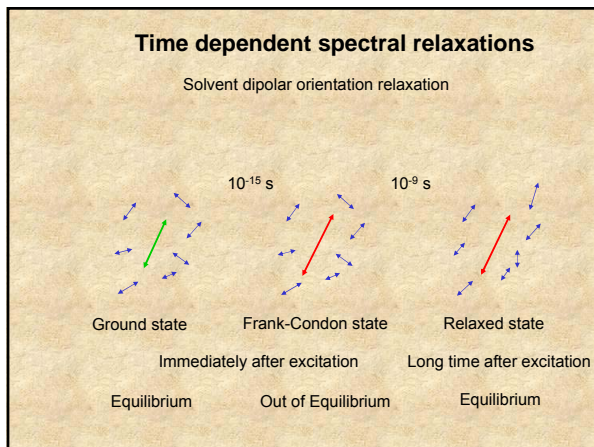
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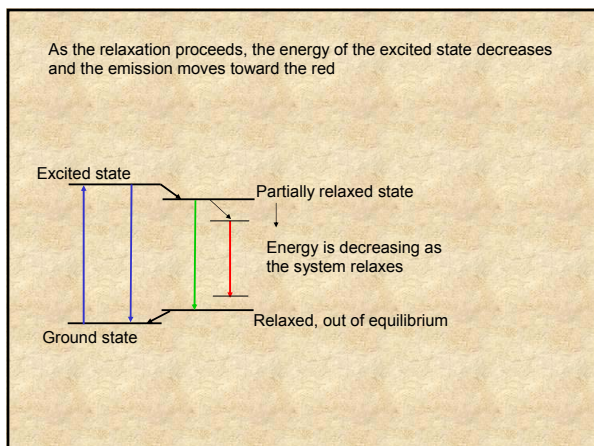
Discrete
Local chi-square = 1.080
Fr_ex donor 1->0 = V 0.33
Fr_em donor 1->0 = V 0.00
Tau donor 1->0 = F 5.00
Tau acceptor 1->0 = F 2.00
Distance D to A 1->0 = F 40.00
Ro (in A) 1->0 = F 40.00
Distance width 1->0 = V 0.58

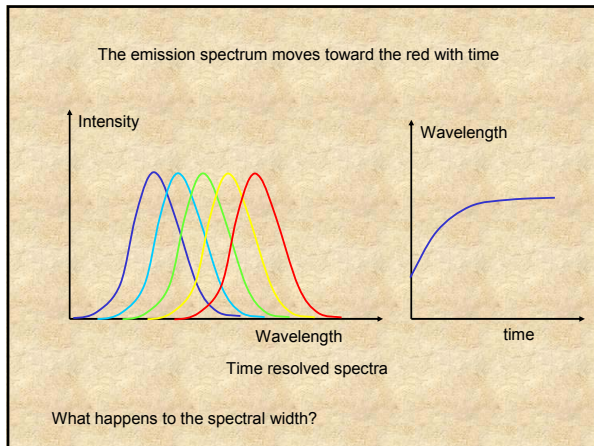
Gaussian distributed
Local chi-square = 1.229
Fr_ex donor 1->0 = V 0.19
Fr_em donor 1->0 = V 0.96
Tau donor 1->0 = L 5.00
Tau acceptor 1->0 = L 2.00
Distance D to A 1->0 = L 40.00
Ro (in A) 1->0 = L 40.00
Distance width 1->0 = V 26.66
  
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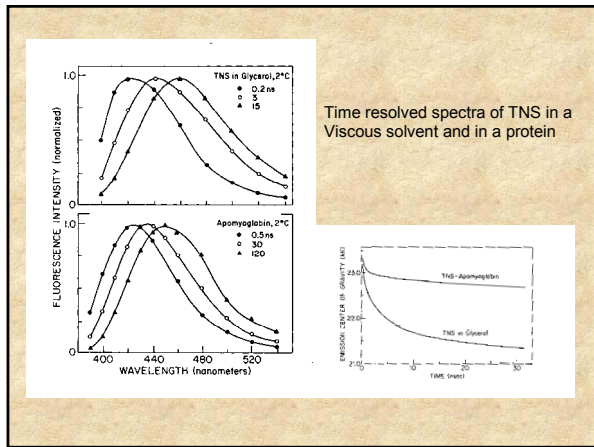
FRET-decay, discrete and distance gaussian distributed
 Fit attempt using 2-exponential linked
 The fit is "poor" using sum of exponentials linked. However, the fit is good if the exponentials are not linked, but the values are unphysical

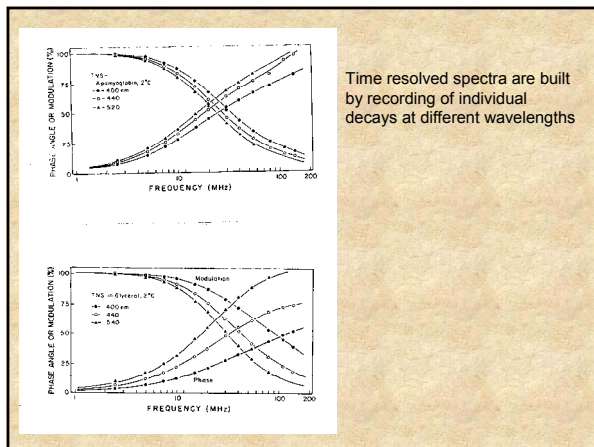


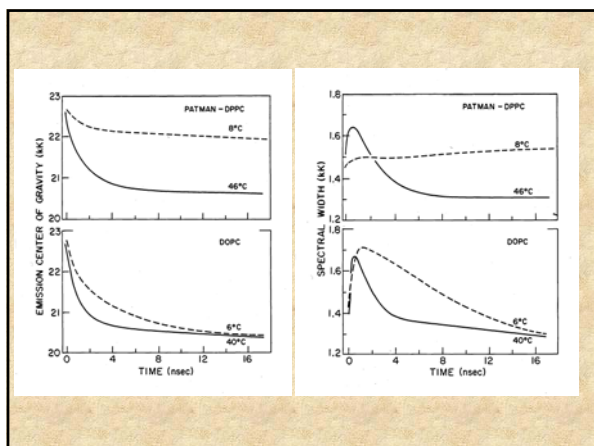


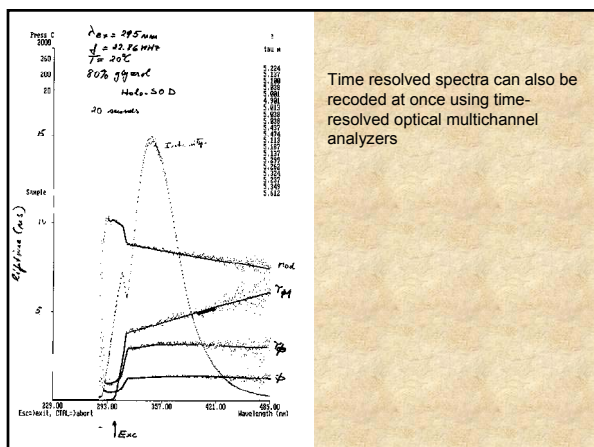






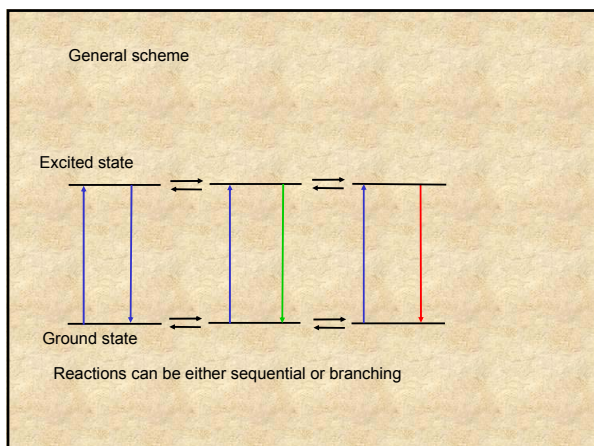






Excited-state reactions

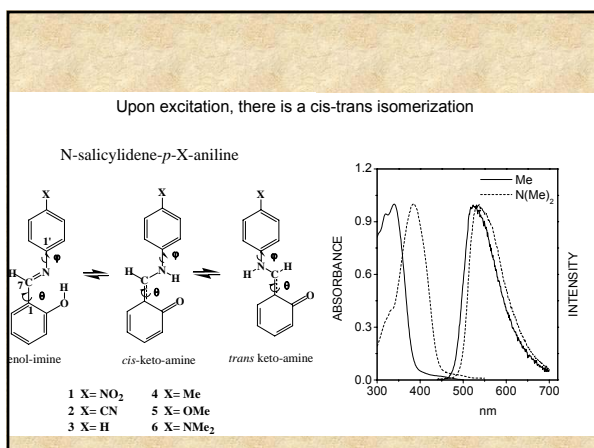
- Excited state protonation-deprotonation
- Electron-transfer ionizations
- Dipolar relaxations
- Twisting-rotations isomerizations
- Solvent cage relaxation
- Quenching
- Dark-states
- Bleaching
- FRET energy transfer
- Monomer-Excimer formation

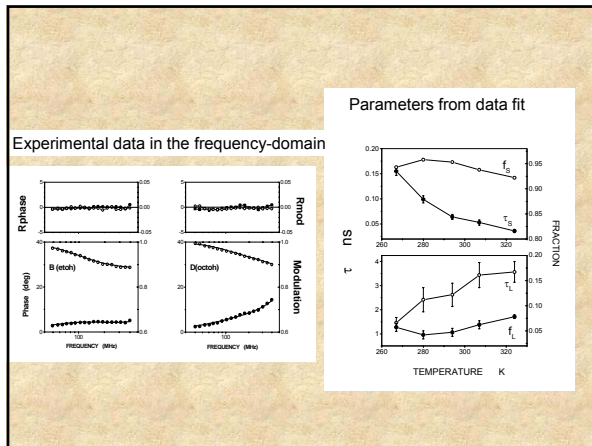


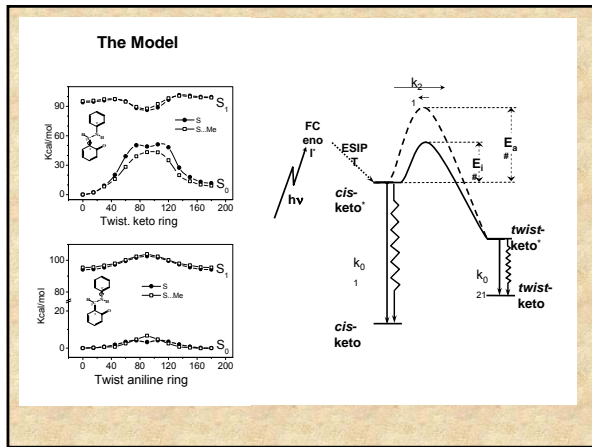
If the reaction rates are **constant**, then the solution of the dynamics of the system is a **sum of exponentials**. The number of exponentials is equal to the number of states

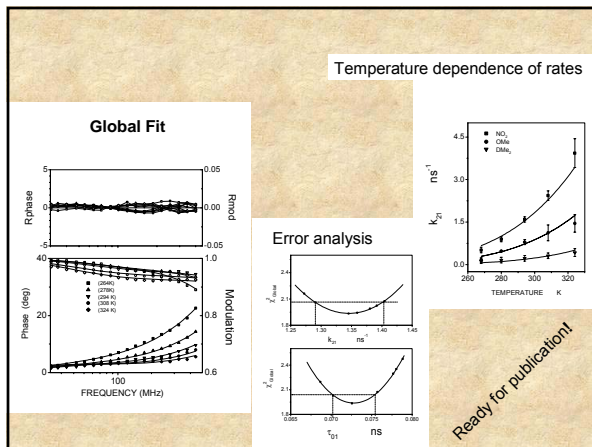
If the system has two states, the decay is doubly exponential

Attention: None of the decay rates correspond to the lifetime of the excited state nor to the reaction rates, but they are a combination of both









Sources on polarization and time-resolved theory and practice:

Books:

Molecular Fluorescence (2002) by Bernard Valeur
Wiley-VCH Publishers

Principles of Fluorescence Spectroscopy (1999) by Joseph Lakowicz
Kluwer Academic/Plenum Publishers

Edited books:

Methods in Enzymology (1997) Volume 278 Fluorescence Spectroscopy (edited by L. Brand and M.L. Johnson)

Methods in Enzymology (2003) Biophotonics (edited by G. Marriott and I. Parker)

Topics in Fluorescence Spectroscopy: Volumes 1-6
(edited by J. Lakowicz)
